

$$1. P = An^3 + \frac{BL^2}{n} \rightarrow \frac{dP}{dn} = P' = 3An^2 - \frac{BL^2}{n^2}$$

$$\underline{CP'_s}: P' = 0 \quad \text{solve for } n. \quad \text{get } n_p = \sqrt[4]{\frac{BL^2}{3A}}$$

$$2. E = \frac{P}{n} = \frac{1}{n} \left(An^3 + \frac{BL^2}{n} \right) = An^2 + \frac{BL^2}{n^2}$$

$$\frac{dE}{dn} = E'(n) = 2An - \frac{2BL^2}{n^3} \quad \text{set} = 0 \quad \text{and solve for } n.$$

$$\text{get } n_E = \sqrt[4]{\frac{BL^2}{A}}$$

$$3. \underbrace{\left(1 - \frac{1}{\sqrt[4]{3}}\right) \sqrt[4]{\frac{BL^2}{A}}}_{\approx 0.241 \dots} \quad \text{is the difference}$$

$$\approx 0.241 \dots$$

4. verify,

$$5. \frac{d\bar{P}}{dx} = A_w n^3 - \frac{Bm^2 g^2}{n x^2} \quad \text{set} = 0 \quad \text{and solve for } x.$$

$$\text{get } x_m = \sqrt{\frac{Bm^2 g^2}{A_w n^4}}$$

As $n \uparrow$ $x_m \downarrow$

$$6. \bar{E} = \frac{\bar{P}}{n}. \quad \frac{d\bar{E}}{dx} = 0 \quad \text{get } x_{\bar{m}} = \sqrt{\frac{Bm^2 g^2}{A_w n^4}}$$
