

**Instructions.** Complete all problems, showing enough work. All work must be done on this paper. You may use your own hand-written notes, but you may not use any electronic devices.

1. [20 points] Consider the initial value problem

$$\begin{cases} y' = y(3 - ty), \\ y(0) = \frac{1}{2}. \end{cases}$$

Use Euler's method with a step size of  $h = \frac{1}{2}$  to complete the table.

k	$t_k$	$y_k$
0		
1		
2		
3		
4		

**2.** [10 points] Find a differential equation whose general solution is

$$y(t) = C_1 e^{2t} + C_2 e^{-3t}.$$

**3.** [30 points] Solve the initial value problem,

$$\begin{cases} y'' + 8y' - 9y = 0, \\ y(1) = 1, \ y'(1) = 0. \end{cases}$$

**4.** [10 points] Write the number  $e^{\ln(2)-\frac{\pi}{6}i}$  in the form a+bi.

**5.** [30 points] Solve the initial value problem,

$$\begin{cases} y'' - 2y' + 5y = 0, \\ y(0) = 2, \ y'(0) = -3. \end{cases}$$

